

Given:

$$3x - 2 = 7$$

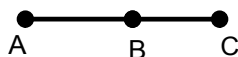
$$\begin{array}{r} + 2 = + 2 \quad \text{reflexive Property} \\ \hline 3x - 2 + 2 = 7 + 2 \quad \text{addition} \\ 3x = 9 \end{array}$$

3.7 The postulates of Addition and subtraction

- **Partition** postulate - A whole is equal to the sum of it's parts
 ★ write horizontal & vertical

This postulate applies to:

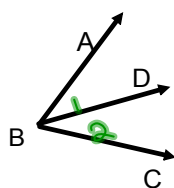
- Line Segments (any number, any length, congruence, measure)



$$\textcircled{1} \overline{AC} \cong \overline{AB} + \overline{BC}$$

$$\textcircled{2} \overline{AC} \\ \overline{AB} + \overline{BC}$$

- Angles (ADJACENT, any number, any measure, congruence, measure)



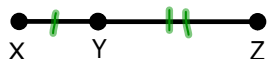
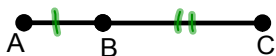
$$\textcircled{1} m\angle 1 + m\angle 2 = m\angle ABC$$

$$\textcircled{2} m\angle 1 + m\angle 2 \\ m\angle ABC$$

- **Addition postulate** - If equal quantities are added to equal quantities, then their sums are equal.
[If $a = b$ and $c = d$ then, $a + c = b + d$]

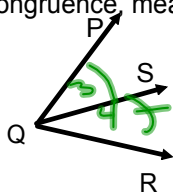
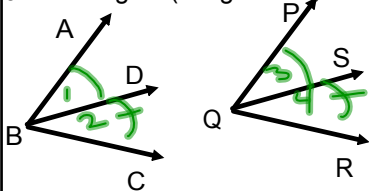
This postulate applies to:

- Line Segments of the same line (congruence, measure)



$$\begin{array}{l} \overline{AB} \cong \overline{XY} \quad \text{Given} \\ \overline{BC} \cong \overline{YZ} \quad \text{Given} \\ \hline \overline{AB} + \overline{BC} \cong \overline{XY} + \overline{YZ} \quad \text{addition} \\ \overline{AC} \cong \overline{XZ} \quad \text{partition} \end{array}$$

- Angles (congruence, measure)



$$\begin{array}{l} m\angle 1 = m\angle 3 \quad \text{Given} \\ m\angle 2 = m\angle 4 \quad \text{Given} \\ \hline m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4 \quad \text{addition} \\ m\angle ABC = m\angle PQR \quad \text{partition} \end{array}$$

- **Subtraction postulate** - If equal quantities are subtracted from equal quantities, then their differences are equal. [If $a = b$ and $c = d$ then, $a - c = b - d$]

★ We never write '-' in proofs.

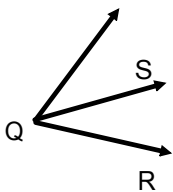
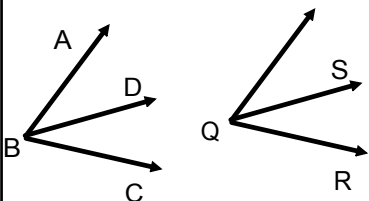
This postulate applies to:

- Line Segments (congruence, measure)

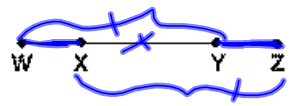


$$\begin{array}{l} \overline{AC} \cong \overline{XZ} \quad \text{Given} \\ \overline{AB} + \overline{BC} \cong \overline{XY} + \overline{YZ} \quad \text{partition} \\ \hline \overline{AB} \cong \overline{XY} \quad \text{Given} \\ \overline{BC} \cong \overline{YZ} \quad \text{Subtraction} \end{array}$$

- Angles (congruence, measure)

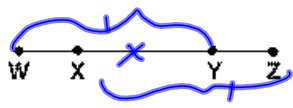


method 1 - partition with substitution

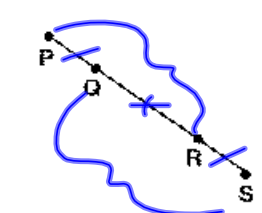


Statements	Reasons
1. $WY = XZ$	1. <u>GIVEN</u>
2. $WX + XY = WY$ $XY + YZ = XZ$	2. <u>partition</u>
3. $WX + XY = XY + YZ$	3. <u>Substitution</u>
4. $XY = XY$	4. <u>reflexive Property</u>
5. $WX = YZ$	5. <u>Subtraction</u>

method 2 - partition without substitution



Statements	Reasons
1. $WY = XZ$	1. <u>GIVEN</u>
2. $WX + XY = XY + YZ$	2. <u>partition</u>
3. $XY = XY$	3. <u>reflexive Property</u>
4. $WX = YZ$	4. <u>Subtraction</u>



Statements

Reasons

1. $PQ = RS$

1. GIVEN

2. $QR = QR$

2. reflexive Property

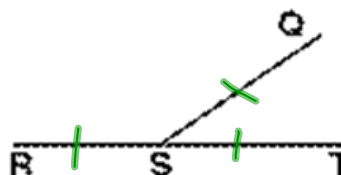
3. $PQ + QR = QR + RS$

3. addition

4. $PR = QS$

4. partitionGiven: S is the midpoint of \overline{RT}

$ST = SQ$

Prove: $RT = SQ + ST$ 

Statements

Reasons

1. S is the midpoint of \overline{RT} 1. given

$ST = SQ$

2. if a point is a midpt it makes 2 = segments.

2. $RS = ST$

3. transitive property

3. $RS = SQ$

4. partition

4. $RT = RS + ST$

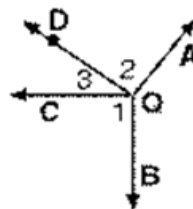
5. Substitution

5. $RT = SQ + ST$

□

Given: $\overrightarrow{QA} \perp \overrightarrow{QD}$
 $\overrightarrow{QB} \perp \overrightarrow{QC}$

Prove: $\angle BQD \cong \angle AQC$



Statements	Reasons
1. $\overrightarrow{QA} \perp \overrightarrow{QD}$ $\overrightarrow{QB} \perp \overrightarrow{QC}$	1. _____
2. $\angle 1, \angle 2$ are right \angle 's	2. _____
3. $\angle 1 \cong \angle 2$	3. _____
4. $\angle 3 \cong \angle 3$	4. _____
5. $\angle 1 + \angle 3 \cong \angle 2 + \angle 3$	5. _____
6. $\angle BQD \cong \angle AQC$	6. _____

Using Partition with Addition and Subtraction

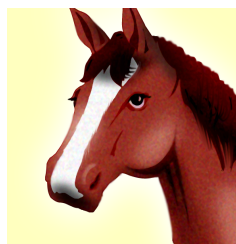
Partition

Addition

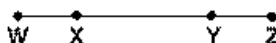
*alphabetical order
 *no '-'

Subtraction

Homework: worksheet



The Partition-Partition Substitution method...



Statements	Reasons
1. $WY = XZ$	1. <u>GIVEN</u>
2. $WY = WX + XY$ $XZ = XY + YZ$	2. <u>partition</u>
3. $WX + XY = XY + YZ$	3. <u>substitution</u>
4. $XY = XY$	4. <u>reflexive property</u>
5. $WX = YZ$	5. <u>subtraction</u>

